General Certificate of Education June 2010

Mathematics
MPC4

Pure Core 4

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## Key to mark scheme and abbreviations used in marking



## No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded. However, there are situations in some units where part marks would be appropriate, particularly when similar techniques are involved. Your Principal Examiner will alert you to these and details will be provided on the mark scheme.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award full marks. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn no marks.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.
Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns full marks, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains no marks.

Otherwise we require evidence of a correct method for any marks to be awarded.

MPC4

\begin{tabular}{|c|c|c|c|c|}
\hline Q \& Solution \& Marks \& Total \& Comments <br>
\hline 1(a)
(b)(i)
(ii) \& $$
\left.\begin{array}{rl}
\mathrm{f}\left(\frac{1}{4}\right) & =8 \times \frac{1}{64}+6 \times \frac{1}{16}-14 \times \frac{1}{4}-1 \\
& =-4 \\
\mathrm{~g}\left(\frac{1}{4}\right) & =\text { number(s) }+d=0 \\
d=3
\end{array}\right] \begin{aligned}
\mathrm{g}(x) & =(4 x-1)\left(2 x^{2}+b x-3\right) \\
x^{2} \quad \begin{array}{lll}
6 & =4 b-2 & \text { or } x \\
b & =2
\end{array} & -14=-b-12
\end{aligned}
$$ \& $$
\begin{gathered}
\text { M1 } \\
\text { A1 } \\
\text { M1 } \\
\text { A1 } \\
\text { B1F } \\
\text { M1 } \\
\text { A1 }
\end{gathered}
$$ \& 2
2

3 \& | Use $x=\frac{1}{4}$ in evaluation |
| :--- |
| NMS 2/2; no ISW |
| Use factor theorem to find $d$ See some processing NMS 2/2 $a=2 \quad c=-3 ; \text { F on } d(c=-d)$ |
| Any appropriate method; PI NMS 2/2 | <br>

\hline \& Total \& \& 7 \& <br>
\hline (a)

(b)(i) \& \begin{tabular}{l}
Alternatives:
$$
\begin{array}{r}
4 x - 1 \longdiv { 2 x ^ { 2 } + 2 x - 3 } \begin{array} { r } 
{ 8 x ^ { 3 } + 6 x ^ { 2 } - 1 4 x - 1 } \\
{ 8 x ^ { 3 } \frac { - 2 x ^ { 2 } } { 8 x ^ { 2 } } } \\
{ 8 x ^ { 2 } - 1 4 x } \\
{ \frac { - 1 2 x } { - 1 2 x } } \\
{ - 1 2 x + 3 } \\
{ - 4 }
\end{array}
\end{array}
$$ <br>
Division as for (a) $\Rightarrow d-3$ last line $d=3$

 \& 

(M1) <br>
(A1) <br>
(M1) <br>
(A1)
\end{tabular} \& (2)

(2) \& | Complete division with integer remainder |
| :--- |
| Remainder $=-4$ stated |
| Candidate's -3 | <br>

\hline 2(a) \& | $\begin{aligned} & \begin{aligned} \frac{\mathrm{d} x}{\mathrm{~d} t} & =-3 \quad \frac{\mathrm{~d} y}{\mathrm{~d} t}=6 t^{2} \\ \frac{\mathrm{~d} y}{\mathrm{~d} x} & =-\frac{6 t^{2}}{3} \\ & =-2 t^{2} \end{aligned} \\ & t=1 \quad m_{\mathrm{T}}=-2 \quad m_{\mathrm{N}}=\frac{1}{2} \end{aligned}$ |
| :--- |
| Attempt at equation of normal using $(x, y)=(-2,3)$ |
| Normal has equation $y-3=\frac{1}{2}(x+2)$ $\begin{aligned} & t=\frac{1-x}{3} \quad \text { or } \quad t=\sqrt[3]{\frac{y-1}{2}} \\ & y=1+2\left(\frac{1-x}{3}\right)^{3} \end{aligned}$ | \& | B1 |
| :--- |
| M1 |
| A1 |
| M1 |
| A1F |
| M1 |
| A1 |
| M1 |
| A1 | \& 3

4
4

2 \& | Both derivatives correct; PI |
| :--- |
| Correct use of chain rule |
| CSO |
| Substitute $t=1 \quad m_{N}=-\frac{1}{m_{T}}$ |
| F on gradient; $m_{\mathrm{T}} \neq \pm 1$ |
| Condone one error |
| CSO; ACF |
| Correct expression for $t$ in terms of $x$ or $y$ |
| ACF | <br>

\hline \& Total \& \& 9 \& <br>
\hline
\end{tabular}

\begin{tabular}{|c|c|c|c|c|}
\hline Q \& Solution \& Marks \& Total \& Comments \\
\hline 3(a)(i) \& \[
\begin{aligned}
\& 7 x-3=A(3 x-2)+B(x+1) \\
\& x=-1 \quad x=\frac{2}{3} \\
\& A=2 \quad B=1 \\
\& \begin{array}{r}
\int \frac{7 x-3}{(x+1)(3 x-2)} \mathrm{d} x= \\
p \ln (x+1)+q \ln (3 x-2) \\
= \\
2 \ln (x+1)+\frac{1}{3} \ln (3 x-2)(+c)
\end{array} \\
\& \begin{aligned}
\frac{6 x^{2}+x+2}{2 x^{2}-x+1} \& =\frac{6 x^{2}-3 x+3+4 x-1}{2 x^{2}-x+1} \\
\quad= \& 3+\frac{4 x-1}{2 x^{2}-x+1}
\end{aligned}
\end{aligned}
\] \& \begin{tabular}{l}
M1 m1 A1 \\
M1 \\
A1F \\
M1 \\
B1 \\
A1
\end{tabular} \& 3

2

3 \& | Substitute two values of $x$ and solve for $A$ and $B$ |
| :--- |
| Or solve $\left.\begin{array}{rl}7 & =3 A+B \\ -3 & =-2 A+B\end{array}\right\}$ condone one error |
| Condone missing brackets |
| F on $A$ and $B$; constant not required $\begin{aligned} & P=3 \\ & Q=4 \text { and } R=-1 \end{aligned}$ | <br>

\hline \& Total \& \& 8 \& <br>

\hline (a)(i) \& | Alternatives: |
| :--- |
| By cover up rule $\begin{aligned} & x=-1 \quad A=\frac{-7-3}{-5} \\ & x=\frac{2}{3} \quad B=\frac{\frac{14}{3}-3}{\frac{5}{3}} \\ & A=2 \quad B=1 \\ & 2 x ^ { 2 } - x + 1 \longdiv { 6 x ^ { 2 } + x + 2 } \\ & \frac{6 x^{2}-3 x+3}{4 x-1} \end{aligned}$ |
| or $\begin{aligned} & 6 x^{2}+x+2=P\left(2 x^{2}-x+1\right)+Q x+R \\ & \quad=2 P x^{2}+(Q-P) x+P+R \\ & P=3 \\ & Q-P=1 \\ & P+R=2 \\ & Q=4 \text { and } R=-1 \end{aligned}$ | \& | (M1) |
| :--- |
| (A1,A1) |
| (M1) |
| (B1) |
| (A1) |
| (M1) |
| (B1) |
| (A1) | \& (3)

(3)

(3) \& | $x=-1 \text { and } x=\frac{2}{3}$ |
| :--- |
| and attempt to find $A$ and $B$ |
| SC NMS $A$ and $B$ both correct $3 / 3$ |
| One of $A$ or $B$ correct $1 / 3$ |
| Complete division, with $a x+b$ remainder |
| $P=3$ stated |
| $Q=4$ and $R=-1$ stated or written as expression |
| Multiply across and equate coefficients or use numerical values of $x$ $P=3$ stated |
| $Q=4$ and $R=-1$ stated or written as expression | <br>

\hline
\end{tabular}

MPC4 (cont)


## MPC4 (cont)




## MPC4 (cont)




